



*An Introduction to Input-Output LCA
Theory and Methodology,
its Strengths and Weaknesses
and a Comparison between
Input-Output LCA and Process LCA*

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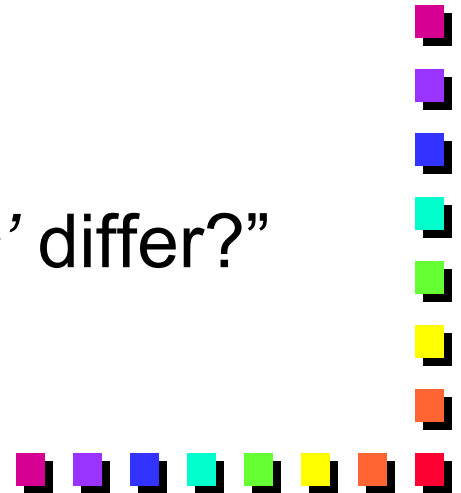
Sylvatica / Harvard University / U. New Hampshire
USA



My Assumptions

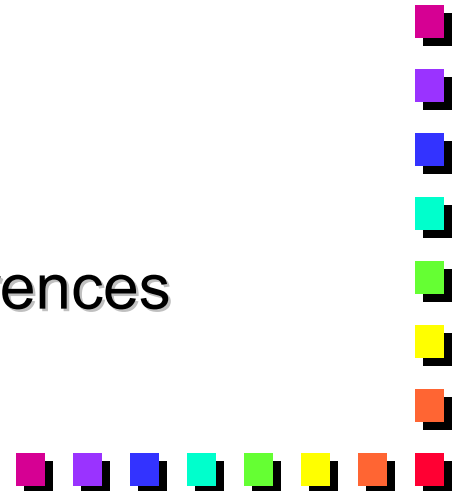
- Know Process LCI
 - Know enough about IO-LCI to be interested
-

- “How do PLCI and IO-LCI *‘inputs’* differ?”
 - Methods
 - Data sources
 - Assumptions
- “How does IO-LCI work?”
- “How do PLCA and IO-LCI *‘outputs’* differ?”
 - Results, conclusions, uncertainties
 - Applications

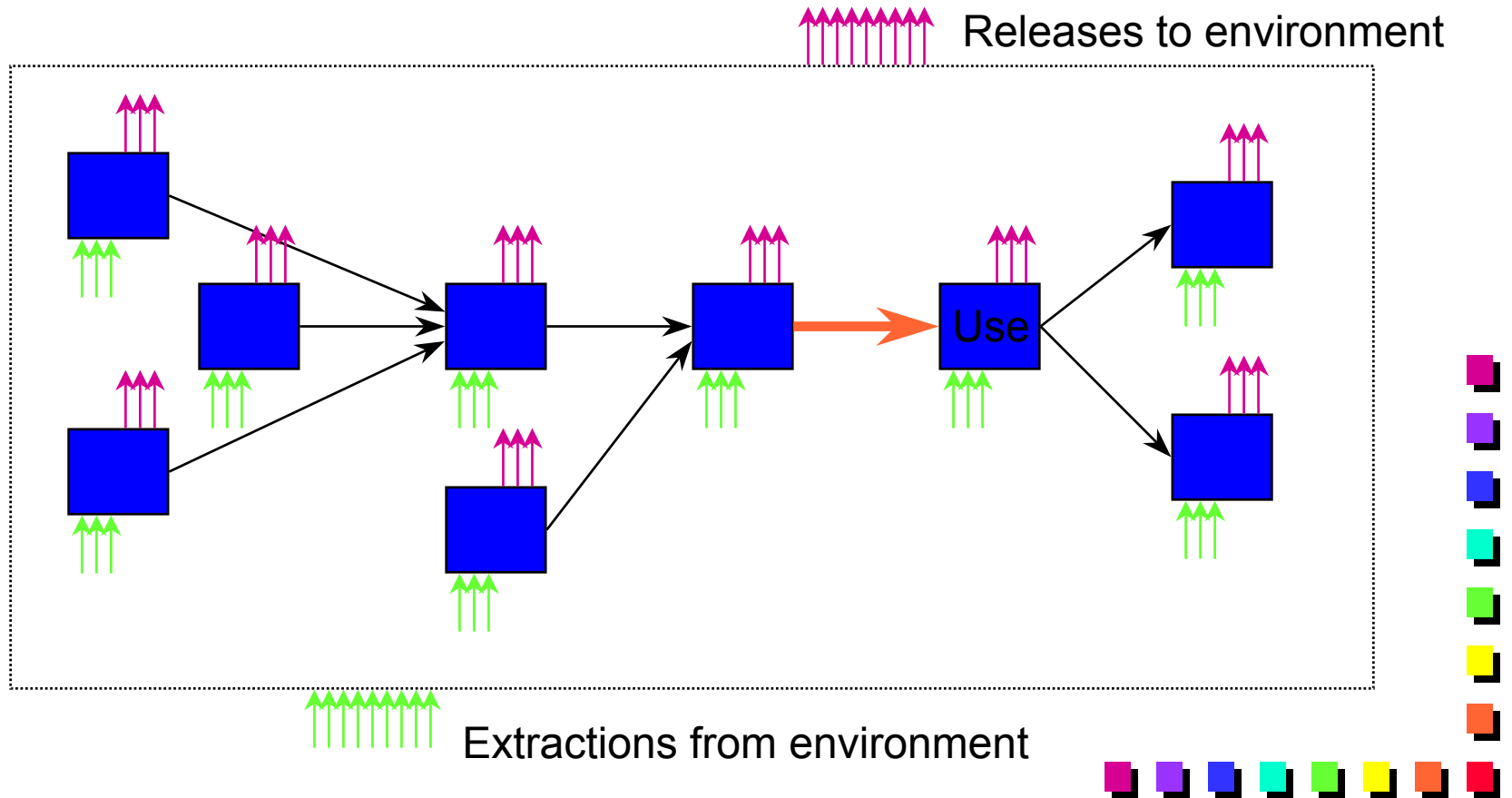


Outline

- Product LCI Reconsidered
 - Essentials
 - Matrix framing
- IO-LCI vis-à-vis Product LCI
- Differences
 - Data
 - Outcomes
- My Purposes:
 - Strip away misconceptions about differences
 - Focus on true remaining differences



Life Cycle Inventory Analysis



Unit Process defined

- ISO 14040: The level of detail at which life cycle inventory data are gathered.
 - Boiler
 - Coal steam power plant
- Note that PLCI databases usually report average data across a sample
 - Oil-fired industrial boilers
 - US coal steam power plants

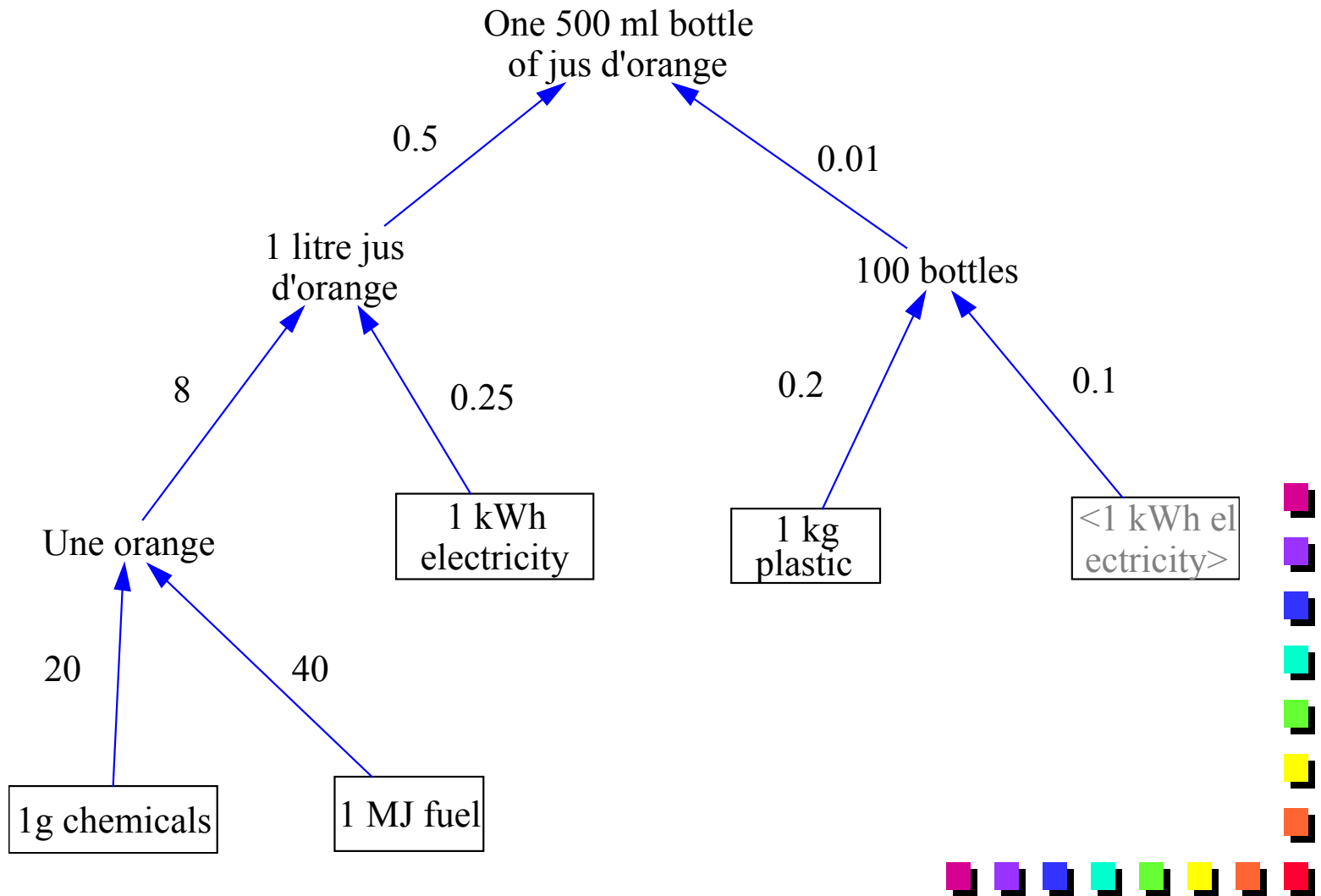


Unit Process, PLCI

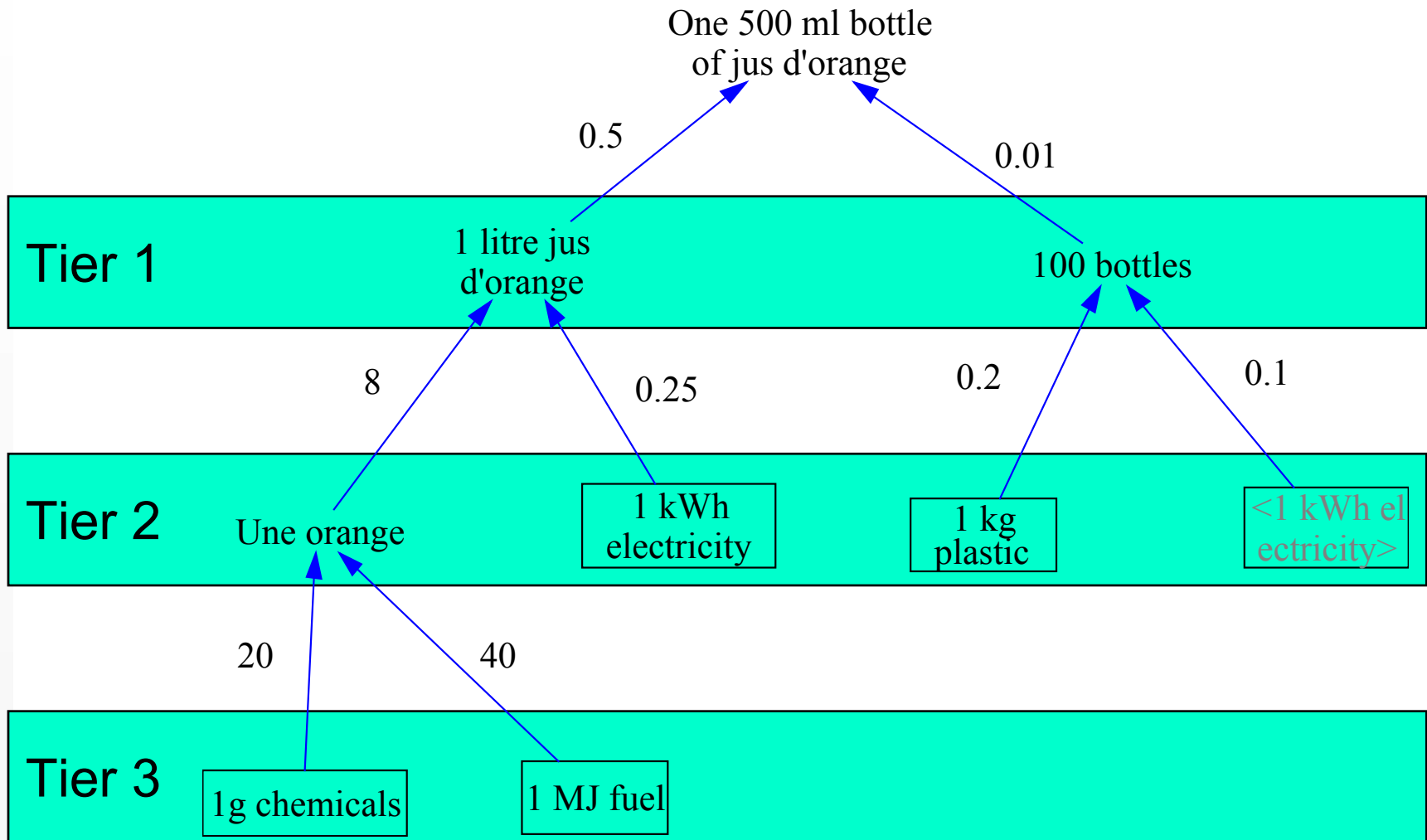
Data		
PRODUCTS		
Known outputs to technosphere. Products and co-products		
Name	Amount	Unit
Known outputs to technosphere. Avoided products		
Name	Amount	Unit
INPUTS		
Known inputs from nature (resources)		
Name	Amount	Unit
Known inputs from technosphere (materials/fuels)		
Name	Amount	Unit
Known inputs from technosphere (electricity/heat)		
Name	Amount	Unit
OUTPUTS		
Emissions to air		
Name	Amount	Unit
Emissions to water		
Name	Amount	Unit
Emissions to soil		
Name	Amount	Unit
Solid emissions		
Name	Amount	Unit
Non material emissions		
Name	Amount	Unit
Known outputs to technosphere. Waste and emissions to treatment		
Name	Amount	Unit



PLCI "Process Tree"



PLCI "Process Tree"



Assume for simplicity that each process has unit emissions of 1 kg / specified output.

We can solve for the LCI using a matrix formulation of the problem

Result - Ind by Ind Direct Requirements

Mid Value of Ind by Ind Direct Requirements

Supplying Inds Totals

Using Inds Totals

	1 500ml bottle juice	1 liter juice	100 bottles	1 orange	1 kg plastic	1 g chemicals	1 kWh electricity	1 MJ fuel
1 500ml bottle juice	0	0	0	0	0	0	0	0
1 liter juice	0.5	0	0	0	0	0	0	0
100 bottles	0.01	0	0	0	0	0	0	0
1 orange	0	8	0	0	0	0	0	0
1 kg plastic	0	0	0.2	0	0	0	0	0
1 g chemicals	0	0	0	20	0	0	0	0
1 kWh electricity	0	0.25	0.1	0	0	0	0	0
1 MJ fuel	0	0	0	40	0	0	0	0

A =

y =

$$\begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Tier 1 output = Ay

Tier 2 output = A(Ay) = A²y

Tier 3 output = A(A(Ay)) = A³y

...

Total output x = y + Ay + A²y + A³y + ...

x = (I + A + A² + A³ + A⁴ + ...)x = (I - A)⁻¹y

Also via: x = Ax + y → (I - A)x = y



Output results

Result - Tierwise Reqts								
Mid Value of Tierwise Reqts								
Supplying Inds <input type="checkbox"/> Totals								
Tier <input checked="" type="checkbox"/> Totals								
	0	1	2	3	4	5	6	Totals
1 500ml bottle juice	1	0	0	0	0	0	0	1
1 liter juice	0	0.5	0	0	0	0	0	0.5
100 bottles	0	0.01	0	0	0	0	0	0.01
1 orange	0	0	4	0	0	0	0	4
1 kg plastic	0	0	2m	0	0	0	0	2m
1 g chemicals	0	0	0	80	0	0	0	80
1 kWh electricity	0	0	0.126	0	0	0	0	0.126
1 MJ fuel	0	0	0	160	0	0	0	160

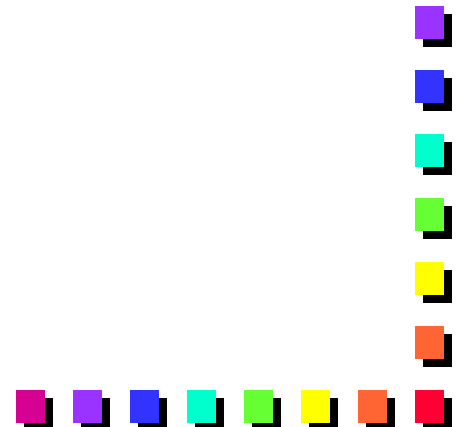
$e \equiv \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$

Tier 1 inventory = $e^T[Ay]$

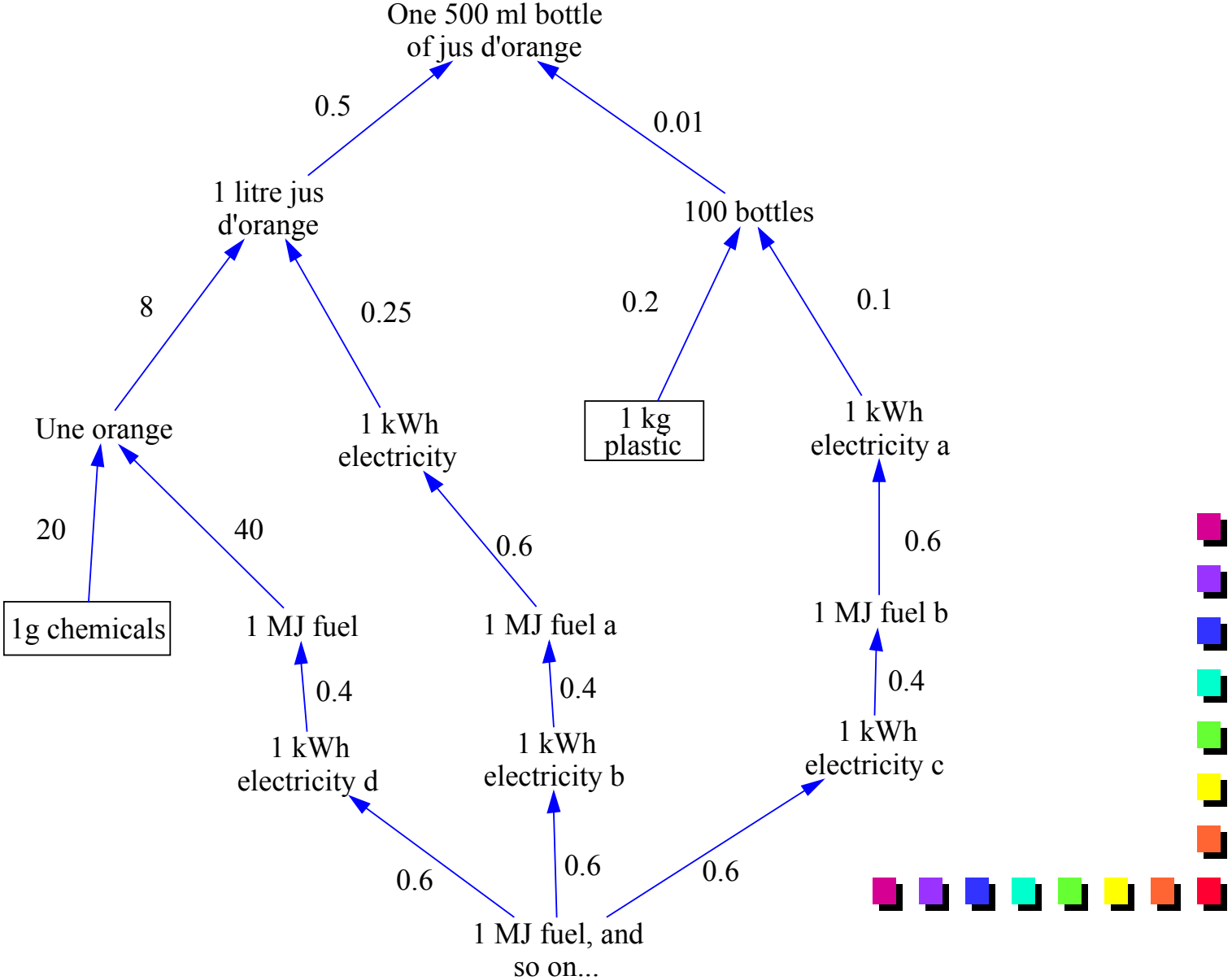
Tier 2 inventory = $e^T[A(Ay)] = e^T[A^2y]$

...

Total inventory = $e^T x = e^T(I-A)^{-1}y$



Process tree with loops... no difficulty for matrix method



A =

Edit Table - Ind by Ind Direct Requirements

Edit Table of Ind by Ind Direct Requirements

Supplying Inds ▼

Using Inds ▼▶

	1 500ml bottle juice	1 liter juice	100 bottles	1 orange	1 kg plastic	1 g chemicals	1 kWh electricity	1 MJ fuel
1 500ml bottle juice	0	0	0	0	0	0	0	0
1 liter juice	0.5	0	0	0	0	0	0	0
100 bottles	0.01	0	0	0	0	0	0	0
1 orange	0	8	0	0	0	0	0	0
1 kg plastic	0	0	0.2	0	0	0	0	0
1 g chemicals	0	0	0	20	0	0	0	0
1 kWh electricity	0	0.25	0.1	0	0	0	0	0.4
1 MJ fuel	0	0	0	40	0	0	0.6	0



Tier-wise output =

Result - Tierwise Reqts

mid
 1.2 Mid Value of Tierwise Reqts
 Supplying Inds Totals
 Tier Totals

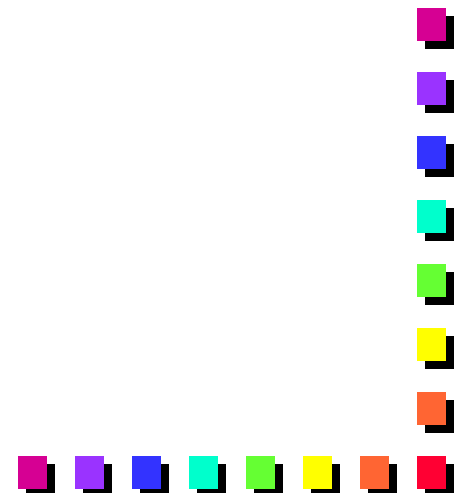
	0	1	2	3	4	5	6	7
1 500ml bottle juice	1	0	0	0	0	0	0	0
1 liter juice	0	0.5	0	0	0	0	0	0
100 bottles	0	0.01	0	0	0	0	0	0
1 orange	0	0	4	0	0	0	0	0
1 kg plastic	0	0	2m	0	0	0	0	0
1 g chemicals	0	0	0	80	0	0	0	0
1 kWh electricity	0	0	0.126	0	64.03	0	15.37	0
1 MJ fuel	0	0	0	160.1	0	38.42	0	9.22

$$x = (I-A)^{-1}y =$$

Result - Vector of Total Requirements

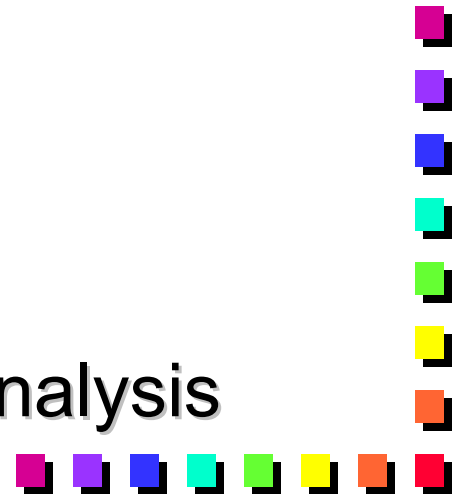
mid
 1.2 Mid Value of Vector of Total Requirements
 Supplying Inds Totals

1 500ml bottle juice	1
1 liter juice	0.5
100 bottles	0.01
1 orange	4
1 kg plastic	2m
1 g chemicals	80
1 kWh electricity	84.38
1 MJ fuel	210.6



Subsequent slides:

- How do we develop the PLCI data?
- IO-LCA Data basis
- IO-LCA matrix model form and example
- If PLCA and IO-LCA are mathematically equivalent, why is IO-LCA interesting?
 - Data
 - Already collected
 - Comprehensive on inputs
 - Comprehensive on products
- Strengths, weaknesses of each
- Examples of boundary truncation analysis with IO LCA



Flexibility in Scope of Input Type

- Material / Energy inputs - major
- Equipment, capital, infrastructure - major
- Material / Energy inputs - minor
- Overhead inputs (building, site, etc.)
- Service inputs
- Personnel-related expenses (travel, hotels...)
- Work-related employee expenditures (car,...)
- Delta-consumption due to employment demand
- (X) Total consumption of employees
- Profits (spending / re-investment)
- Taxes (spent by government)



Some slides which may also
be used, follow...



Adding Pollution (or any impact): Basic Approach

x_i = sector i economic output (\$/yr)

p_{ij} = sector i pollutant j release (kg/yr)

$$\frac{p_{ij}}{y_i} = e_{ij} = \text{sector } i \text{ pollution intensity (kg/\$)}$$



Data Discussion - USA

- Economic I/O Data
- Energy-related Air Emissions
- Toxic Release Inventory



The “Work Files”

- US Department of Commerce’s Bureau of Economic Analysis (BEA)
- BEA creates the I/O tables from establishment-level Census data
- Work files are an unpublished, intermediate data product
- Most recently published: 1992
- 1997 data projected for 2001
- “Transactions” table: 1000 x 7000 detailed “Use” matrix (use of 7K items by 1K industries)



Energy-related Air Emissions

- CO₂, { CO, NO_x, SO₂, Particulates, VOCs }
- Approaches for estimating P_{ij} (kg/year, each sector, flow)
 - Carnegie-Mellon University approach:
 - \$ fuel per year → kg or litres fuel per year → kg pollutant
 - Sylvatica approach:
 - CO₂: Department of Energy data on fuel *combusted per year*
 - {"Criteria air pollutants"}: US EPA emissions inventories (kg/yr, each sector, each flow)
 - Needed: comparison of results; estimates of uncertainties;
 - Advantages of latter approaches:
 - More recent (1996 vs. 1992)
 - Continual improvement, millions of man-hours at state level
 - Capture non-energy-related process emissions (e.g., VOCs)
 - Avoid allocating combustion to feedstock uses
 - Avoid sectoral price difference impacts
- Main message: data selection and integration = model design



Toxic Release Inventory

- US EPA: Required plant-level annual reporting
- Manufacturing sectors, ~ 300 pollutants
- Need to characterize uncertainties due to:
 - Reporting/measurement/estimation error
 - Non-reporting
 - Non-reporting sectors
 - Non-reporting establishments within reporting sectors
 - Non-reported chemicals from reporting establishments
- Need to create adjusted e_{ij} intensities (kg/\$)

